

# Nonlinear Circuits and Devices

## Logarithmic Amplifier

### Milestone 0

Schokley's first-order theory for a pn-junction gives the relationship between the voltage  $V_D$  across the diode and the current  $I$  as

$$I_D = I_S \left( \exp\left(\frac{eV_D}{k_B T}\right) - 1 \right) \tag{8.1}$$

where  $e = 1.6 \times 10^{-19}$  C,  $k_B = 1.38 \times 10^{-23}$  J K<sup>-1</sup> and  $I_S$  is the **reverse saturation-current** of the diode, typically 25 nA at 25°C but it doubles with every 10°C increase in temperature.

Shockley's model can be improved with the addition of a parameter  $1 < \lambda < 2$  such that

$$I_D \approx I_S \exp\left(\frac{eV_D}{\lambda k_B T}\right) \text{ when } V_D > 100 \text{ mV.} \tag{8.2}$$

Assuming that  $|V_1/R_1| \ll |V_3/R_3|$ , use this approximation to calculate  $V_4$  as a function of  $V_1$  for circuit 8.1 (below). What is (a) the lowest value of  $V_4$ , and (b) the largest value of input current ( $V_1/R_1$ ), for which you would expect the circuit to work satisfactorily?

### Milestone 1

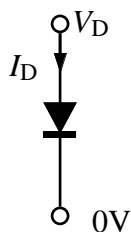
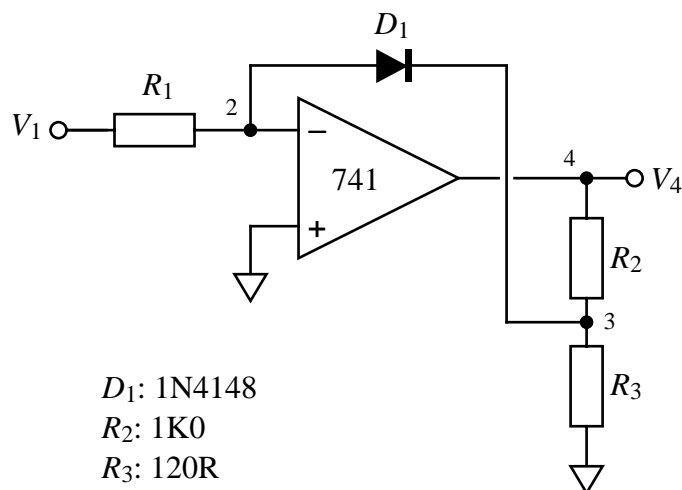
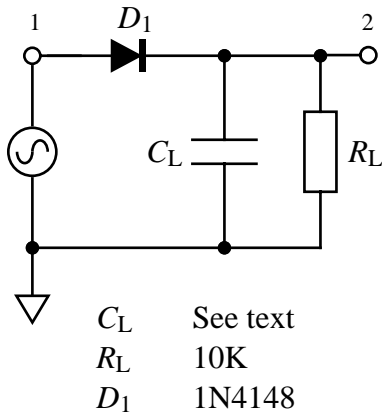


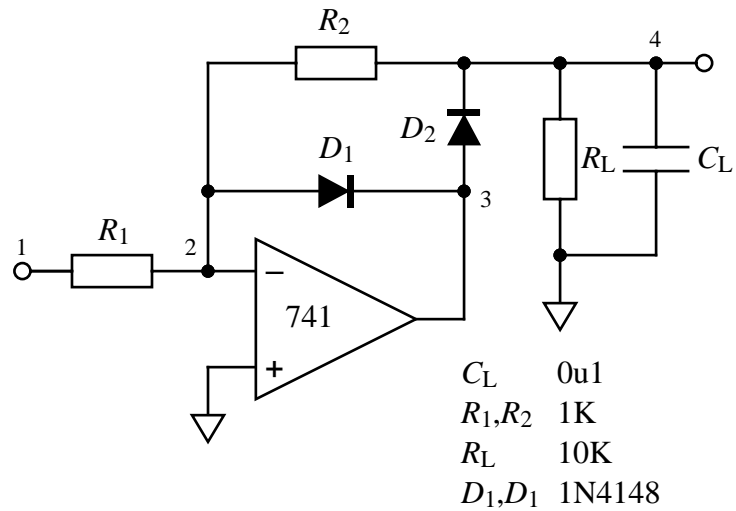
Figure 1. Sign convention.



Circuit 8.1 Primitive logarithmic amplifier



Circuit 8.2 Passive half-wave rectifier



Circuit 8.3 Precision half-wave rectifier

Construct circuit 8.1. Adjust the op-amp offset-null with the diode temporarily bridged by a 1 k $\Omega$  resistor. Test your circuit by plotting a graph (on semi-log axes) of  $V_4$  vs  $V_1/R_1$  over a range from 0.1  $\mu$ A to 1 mA (use values for  $R_1$  of 1 k $\Omega$ , 33 k $\Omega$  and 1 M $\Omega$  to cover the range). Estimate the values of  $\lambda$  and  $I_S$  for the diode, and comment on the accuracy of the model.

### Milestone 2

#### Half-Wave Rectifiers

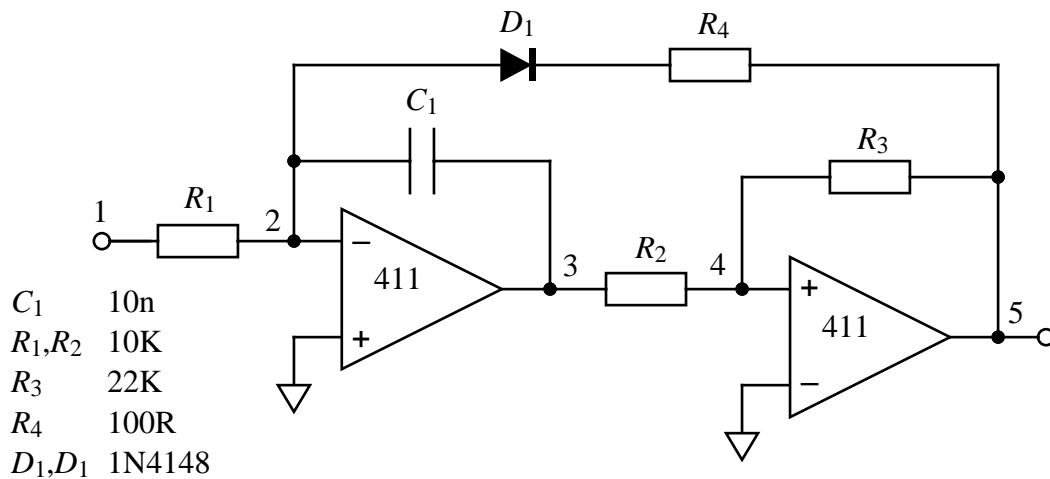
Circuit 8.2 is a so-called **half-wave rectifier**. Build it and, using a 5 V amplitude 2 kHz sine-wave input (node 1), carefully sketch the output (node 2) waveform when the smoothing capacitor  $C$  has each of the values: 0 pF (*i.e.* not present), 10 nF and 100 nF.

With  $C = 100$  nF and a 2 kHz sine-wave input, measure the DC voltage (with a DMM) at the output as a function of the input amplitudes from 0 to 10 V and plot the results on a graph.

### Milestone 3

Construct circuit 8.3 and, as before, with a 2 kHz sine-wave input, measure the DC voltage at the output (node 4) as a function of the input amplitudes. Add the results to your previous graph and comment on the accuracy of this circuit.

### Milestone 4



Circuit 8.4 Simple voltage-to-frequency converter

### Voltage-to-Frequency Converter

Circuit 8.4 is a simple **voltage-to-frequency converter**, the frequency  $f$  of its output depends on the (DC) voltage at the input  $V_{in}$ . Build this circuit and sketch the signals at nodes 3 and 5 when the input is 1 V. Briefly explain how the circuit works and obtain an expression relating  $f$  to  $V_1$ . Plot a graph of the measured  $f$  against  $V_1$ . and hence determine the linearity and range of this circuit. Ask a demonstrator to see whether a frequency counter is available for this part of the experiment as the circuit may well be more accurate than the oscilloscope timebase.

Note: Circuit 8.4 is abusing an *op-amp* by using one as a *comparator*. This is bad practice because op-amps are designed to work with  $V_+ = V_-$  and have poor performance (they may even suffer latch-up, or become noisy) in circuits where this is not the case. Comparators are designed to operate with  $V_+ \ll V_-$  or  $V_+ \gg V_-$  and should be used for this purpose all 'real' applications.

### Milestone 5