

# Monolayers of $^3\text{He}$ on the surface of bulk superfluid $^4\text{He}$

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## Abstract

We have used quantum evaporation to investigate the two-dimensional fermion system that forms at the free surface of (initially isotopically pure)  $^4\text{He}$  when small quantities of  $^3\text{He}$  are added to it. By measuring the first-arrival times of the evaporated atoms, we have determined that the  $^3\text{He}$ - $^3\text{He}$  potential in this system is  $V_{3S}/k_B = 0.23 \pm 0.02 \text{ K nm}^2$  (repulsive) and estimated a value of  $m_{3S} = (1.53 \pm 0.02)m_3$  for the zero-coverage effective mass. We have also observed the predicted second layer-state which becomes occupied once the first layer-state density exceeds about 0.6 monolayers.

*Keywords:* Quantum evaporation; surface; liquid helium; 2-D fermion system

When small quantities of  $^3\text{He}$  are added to bulk superfluid  $^4\text{He}$  below  $T \sim 100 \text{ mK}$  the atoms occupy so-called Andreev states [1] and form a degenerate two-dimensional fermion system. At low temperatures, and when the surface density of  $^3\text{He}$   $n_{3S}$  is less than about half a monolayer, the  $^3\text{He}$  chemical potential can be described [2] by

$$\mu_3 = E_{3S}^{(0)} + \left( \frac{\pi \hbar^2}{m_{3S}} + \frac{V_{3S}}{2} \right) n_{3S} \quad (1)$$

where  $E_{3S}^{(0)}$  is the binding energy of a single  $^3\text{He}$  atom (effective mass  $m_{3S}$ ) to the  $^4\text{He}$  surface.  $V_{3S}$  parameterises the  $^3\text{He}$ - $^3\text{He}$  interaction.

Values of  $m_{3S}$  and  $V_{3S}$  inferred from measurements of thermodynamic properties of the surface, such as surface tension, are strongly covariant (see [3] for example). However, we have been able to obtain independent values for these quantities us-

ing a new method based on quantum evaporation [4,5], as follows:

A tightly collimated beam of high-energy phonons [6] was directed at normal incidence to the free liquid surface (Fig. 1a). The evaporated  $^3\text{He}$  atom beam was also collimated so that only

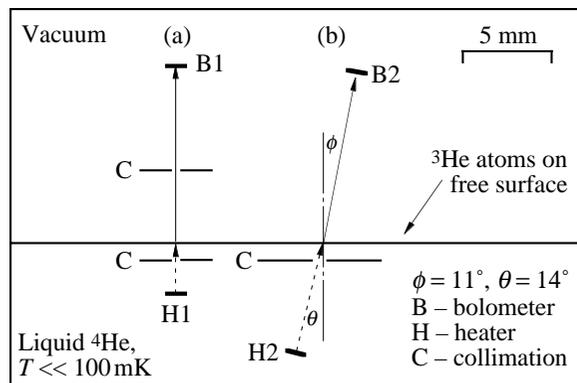


Fig. 1. Schematic diagram of the quantum evaporation experiment

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atoms with a nearly zero component of momentum parallel to the surface were detected. An incident phonon of energy  $E_p$  imparts kinetic energy to the ejected atom, which has bare mass  $m_3$ , such that

$$\frac{1}{2}m_3v^2 - E_p = E_{3S}^{(0)} + \frac{1}{2}V_{3S}n_{3S}. \quad (2)$$

The distribution of phonon energies arriving at the surface is unaffected by  $n_{3S}$  at the coverages used, and the value of  $E_{3S}^{(0)}/k_B = -5.02 \pm 0.03$  K [3] is constant. Therefore, the variation with  $n_{3S}$  of arrival times of  $^3\text{He}$  atoms at the bolometer is due simply to the term  $\frac{1}{2}V_{3S}n_{3S}$  in Eqn 2. Our measured first-arrival times were consistent with Eqn 2 for coverages up to  $n_{3S} = 4 \text{ nm}^{-2}$  (Fig. 2) and we conclude that  $V_{3S}/k_B = (0.23 \pm 0.02) \text{ K nm}^2$ . Knowledge of this value eliminates the uncertainty due to covariance (see above) in the value of  $m_{3S}$  inferred from measurements [3,7] of surface-sound velocity and surface tension. Hence, the best estimate of  $m_{3S}$  can be refined from  $(1.45 \pm 0.10)m_3$  to  $m_{3S} = (1.53 \pm 0.02)m_3$ .

We have also used a slight variant of the experiment (Fig. 1b) to search for evidence of a second ‘excited’ state predicted by Pavloff and Treiner [8]. Atoms in this state have a smaller binding energy  $E_{3S}^{(1)}$  to the surface than those in the first surface state, and the signature of its occupation is therefore an additional faster component in the detected signal. This component appeared, albeit at a level

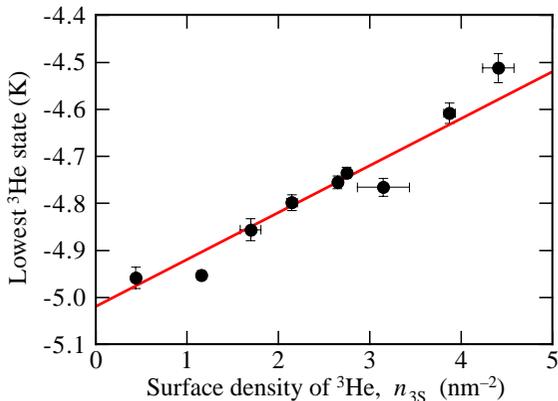


Fig. 2. Values of  $E_{3S}^{(0)} + \frac{1}{2}V_{3S}n_{3S}$  deduced from measured first-arrival times for  $^3\text{He}$  atoms evaporated by high-energy phonons as a function of surface density  $n_{3S}$ .

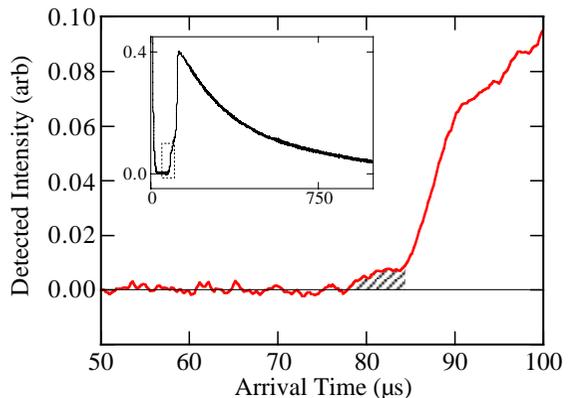


Fig. 3.  $^3\text{He}$  atoms from the lowest surface-state start arriving at  $85 \mu\text{s}$ , the earlier component (shaded) is due to atoms from the excited surface state. The largest signal component (inset) is due to evaporated  $^4\text{He}$  atoms.

not greatly above the detector noise, on all signals taken below  $T = 60 \text{ mK}$  with surface coverages of, and above, about 0.6 monolayers, *i.e.*  $n_{3S} = 4 \text{ nm}^{-2}$  (Fig. 3). From our preliminary measurements of first-arrival times, we find that  $E_{3S}^{(1)} = -3.4 \pm 0.4 \text{ K}$ , in agreement with the predictions [8].

Although this paper has discussed exclusively the states of  $^3\text{He}$  above bulk  $^4\text{He}$ , we note that thin film and layered systems have some comparable properties and have been investigated by other groups using NMR, third-sound and heat capacity measurements [9–11].

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